

Kolumban Hutter · Yongqi Wang ·
Irina P. Chubarenko

Physics of Lakes

Volume 3: Methods of Understanding
Lakes as Components
of the Geophysical Environment



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